

by the contour interval. This approach is more difficult than in the two-dimensional case because the chart must have a variable scale parameter to allow for the different depths of the slabs.

(b) *Analytical methods.* By using an n -sided polygon to approximate the outline of the vertical section of a two-dimensional body, one can calculate the gravity effect by hand or by digital computer (Talwani *et al.*, 1959). A simple section is illustrated in fig. 2.34. It can be shown that the gravity effect of this section is equal to a line integral around the perimeter (Hubbert, 1948). The relation is

$$g = 2\gamma\sigma \oint z \, d\theta.$$

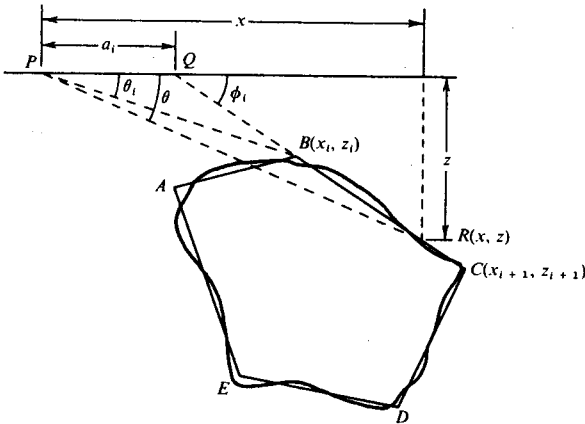


Fig. 2.34 Polygon approximation of irregular vertical section of two-dimensional body.

From the geometry of fig. 2.34 we have the following relations:

$$z = x \tan \theta = (x - a_i) \tan \phi_i, \text{ or } z = (a_i \tan \theta \tan \phi_i) / (\tan \phi_i - \tan \theta).$$

The line integral for the side BC is

$$\int_{BC} z d\theta = \int_B^C \frac{a_i \tan \theta \tan \phi_i}{\tan \phi_i - \tan \theta} d\theta = Z_i.$$

Thus,

$$g = 2\gamma\sigma \sum_{i=1}^n Z_i. \tag{2.54a}$$

In the most general case, Z_i is given by

$$Z_i = a_i \sin \phi_i \cos \phi_i \left[(\theta_i - \theta_{i+1}) + \tan \phi_i \cdot \log \left\{ \frac{\cos \theta_i (\tan \theta_i - \tan \phi_i)}{\cos \theta_{i+1} (\tan \theta_{i+1} - \tan \phi_i)} \right\} \right], \tag{2.54b}$$

From Telford et al. Applied Geophysics, Cambridge U., 800 p., 1976 - Really good background info.

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$$\begin{aligned} \theta_i &= \tan^{-1} \left(\frac{z_i}{x_i} \right), \quad \phi_i = \tan^{-1} \left(\frac{z_{i+1} - z_i}{x_{i+1} - x_i} \right), \quad a_i = x_{i+1} - z_{i+1} \cot \phi_i \\ &= x_{i+1} + z_{i+1} \left(\frac{x_{i+1} - x_i}{z_i - z_{i+1}} \right). \end{aligned}$$

This technique has also been used for three-dimensional bodies by replacing the contours in the horizontal plane with n -sided polygons. The solution, from line integrals of the polygons, is essentially a more complicated version of eq. (2.54a).

Terrain corrections may also be computed by this method. For example, in the three-dimensional case, polygons are fitted to the topographic contours.

2.6.5 Characteristic curves

Most of the formulae for simple gravity shapes are far from simple to apply. Even when we can assume with some confidence that a field result may be reason-